

# Solving One-Variable Equations

## Overview

All lessons are based on solving one-variable equations. The one-variable lessons include:

- Expressions and properties
- Solving equations using properties
- Order of operations (PEMDAS)
- Solving equations using the order of operations
- Solving one-variable inequalities
- Solving absolute value equations and inequalities
- Ratios, proportions, and percents

The number of total suggested days for the unit is 12 to 14.5. Adjustments may be needed based on student performance during the unit and amount of time available until the end of the semester.

## Vocabulary

Integer	Coefficient
Constant	Term
Like terms	Mathematical properties
Numerical expressions	Algebraic expressions
Zero pair	Additive inverse property
Identity property of addition	Multiplicative identity property
Multiplicative property of zero	Multiplicative property of negative one
Reciprocals (inverses)	Multiplicative inverse property
Numerator	Denominator
Commutative property of addition	Associative property of addition
Commutative property of multiplication	Associative property of multiplication
Distributive property	Variable
Unknown	Solution
Addition Property of Equality	Subtraction Property of Equality
Multiplication Property of Equality	Division Property of Equality
Substitution	Substitution Property of Equality
Symmetric	Property of Equality
Input	Output Operations
PEMDAS	GEMDAS
Order of operations	Doing
Undoing	Solve
Solving	OR
AND	Less than
Less than or equal to	Greater than
Greater than or equal to	Inequality
Compound	Compound inequality
Addition Property of Inequality	Subtraction Property of Inequality

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### Vocabulary (Continued)

Multiplication Property of Inequality  
Absolute  
Absolute value inequality  
Proportion  
Percent of change  
Change in value  
Scaled

Division Property of Inequality  
Absolute Value  
Ratio  
Proportional  
Percent  
Original value

### Material List

Student Journal  
Setting the Stage  
Transparencies  
Dry-erase boards  
Markers and erasers  
Overhead tiles  
Student tiles

Tile pad  
Equal tile pad  
Graphing calculators  
Calculator view screen  
Blank transparencies  
Lesson specific  
transparencies

Overhead projector  
Construction paper  
Poster paper and markers  
Graphic organizer  
Scissors  
Centimeter rulers  
Inequality pad

The following table contains lesson name, timeline, summary of concepts covered, and the Essential Question(s) for each lesson.

Lesson	Timeline	Concepts Covered	Essential Question(s)	Common Core Standards for Mathematical Content

<p>Expressions and Properties</p>	<p>2 Days</p>	<ul style="list-style-type: none"> <li>• Represent expressions using:             <ul style="list-style-type: none"> <li>○ symbols</li> <li>○ tiles</li> <li>○ words</li> <li>○ scenarios</li> <li>○ drawings</li> </ul> </li> <li>• Represent equations using:             <ul style="list-style-type: none"> <li>○ symbols</li> <li>○ tiles</li> <li>○ words</li> <li>○ scenarios</li> <li>○ drawings</li> </ul> </li> <li>• Represent and write equivalent expressions</li> <li>• Determine mathematical properties and rules related to expressions and equations</li> </ul>	<p>How can words, symbols, tiles, drawings, and scenarios represent mathematical expressions and equations?</p>	<p>3.OA.5, 5.NF.1, 5.NF.4, 5.OA.1, 5.OA.2, 6.NS.1, 6.NS.5, 6.EE.1, 6.EE.2a, 6.EE.3, 6.EE.6, 7.NS.1a, 7.NS.1c, 7.NS.1d, 7.NS.2a, 7.NS.2b, 7.NS.2c, A-SSE.1a, Modeling</p>
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Solving Equations by Using Properties	1 to 1.5 Days	<ul style="list-style-type: none"> <li>• Solve one-variable equations using the properties of equality:               <ul style="list-style-type: none"> <li>○ Addition</li> <li>○ Subtraction</li> <li>○ Multiplication</li> <li>○ Division</li> </ul> </li> <li>• Check answers using the substitution property of equality</li> <li>• Represent properties of equality using:               <ul style="list-style-type: none"> <li>○ Symbolic equations</li> <li>○ Words</li> <li>○ Numbers</li> <li>○ Tiles</li> </ul> </li> <li>• Translate real-world scenarios into equations to solve</li> </ul>	How can mathematical properties be used to solve equations and real-world applications?	6.EE.5, 6.EE.6, 6.EE.7, 7.EE.2, 7.EE.4a, A-CED.1, A-REI.1, A-REI.2, A-REI.3, Modeling
Order of Operations	2 Days	<ul style="list-style-type: none"> <li>• Evaluate expressions using the order of operations</li> <li>• Create an expression from a series of operations</li> <li>• Determine input needed for an expression to yield a given output</li> </ul>	How can working backward help solve problems in mathematics?	5.OA.1, 5.OA.2, 5.OA.3, 6.EE.1, 6.EE.2, 6.EE.3, 6.EE.4, 7.EE.1, 7.EE.2, 7.EE.3, 8.EE.2, A-SSE.1, Modeling

Solving Equations Using the Order of Operations	1 to 2 Days	<ul style="list-style-type: none"> <li>Solve one-variable equations symbolically using the reverse order of operations and opposite (undo) operations</li> <li>Solve for an unknown in basic real-world applications related to formulas</li> <li>Solve one-variable equations using tables and tiles</li> </ul>	<ul style="list-style-type: none"> <li>How can the order of operations be used to solve equations?</li> <li>How do you solve equations using opposite operations?</li> <li>How do you apply what you have learned about solving equations to solving real-world applications involving formulas?</li> </ul>	6.EE.3, 6.EE.4, 6.EE.5, 6.EE.6, 6.EE.7, 7.EE.1, 7.EE.3, 7.EE.4a, 8.EE.7, A-CED.1, A-REI.1, A-REI.2, A-REI.3, Modeling
Solving One-Variable Inequalities	2 Days	<ul style="list-style-type: none"> <li>Solve one-variable inequalities</li> <li>Graph and describe the solution to one-variable inequalities</li> <li>Solve one-variable inequalities related to real-world applications</li> </ul>	How are solutions to inequalities described in written and graphed formats?	6.NS.6a, 6.NS.7c, 6.NS.7d, 6.EE.5, 6.EE.8, Modeling
Solving Absolute Value Equations and Inequalities	1.5 Days	<ul style="list-style-type: none"> <li>Solve absolute value equations symbolically</li> <li>Solve absolute value inequalities symbolically</li> <li>Graph the solutions to absolute value equations and inequalities on a number line</li> <li>Model real-world phenomena with absolute value equations and inequalities</li> <li>Apply absolute value inequalities to tolerance specifications for consumer products</li> </ul>	<ul style="list-style-type: none"> <li>How can absolute value help model real-world phenomena?</li> <li>How do we solve absolute value equations and inequalities?</li> </ul>	6.NS.6a, 6.NS.7c, 6.NS.7d, 6.EE.5, 6.EE.8, 7.EE.4b, A-CED.1, A-REI.3, Modeling

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Ratios, Proportions and Percent of Change	2 Days	<ul style="list-style-type: none"><li>• Determine percent of change for real-world applications</li><li>• Write the ratio of various real-world applications</li><li>• Use proportions to solve for unknowns in real-world applications</li></ul>	<ul style="list-style-type: none"><li>• How are ratios used to model real-world phenomenon?</li><li>• What are the similarities and/or differences between ratios, proportions, and percent of change?</li></ul>	5.NF.5, 6.RP.1, 6.RP.2, 6.RP.3b, 6.RP.3c, 6.EE.5, 6.EE.6, 7.RP.2a, 7.RP.2b, 7.RP.2c, 7.G.1, 8.G.4, A-CED.1, A-REI.1, G-SRT.2, Modeling
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# Linear Functions

## Overview

All lessons are based on linear functions. The linear function lessons include:

- Plotting Points
- Linear equations and the slope-intercept form
- Applications of linear functions
- Linear function notation
- Other forms of linear functions
- Absolute value functions
- Defining linear functions and the vertical line test
- Linear regression
- Linear inequalities

The total suggested days for the unit is 12 to 14.5. Adjustments may be needed based on student performance during the unit and time available until the end of the semester.

## Vocabulary

Coordinate plane	Table of ordered pairs	Slope intercept	Regression
Cartesian Coordinate Plane	Reflection	Parallel lines	Least sum
$x$ -value	$x$ -minimum	Constant	Correlation coefficient
$y$ -value	$y$ -minimum	Constant rate	Line of best fit
Ordered pair	$x$ -maximum	Term number	Line of least squares
Reflect	$y$ -maximum	Term value	Least-squares line
Scatter plots	$x$ -scale	Input	Correlation
Connected scatter plots	$y$ -scale	Output	Positive correlation
Origin	Original object	Domain	Negative correlation
Intersection	Function	Range	No correlation
Vertical	Input value	Function	Sum
Horizontal	Output value	Function notation	Summation
$x$ -axis	Scenario	Standard form of a linear equation	Summation notation
$y$ -axis	Rule in words	Point-slope form of a linear equation	Linear inequality
Quadrant I	Rule as an equation	Vertical line	Less than
Quadrant II	Graph	Horizontal line	Less than or equal to
Quadrant III	$\Delta x$	Parallel slope	Greater than
Quadrant IV	$\Delta y$	Perpendicular slope	Greater than or equal to
Number line	Slope	Slope-intercept form of a linear equation	Inequality
Positive	Slope of a line	Point	Solution
Negative	Rise	Vertical line test	Solution region
	Run		System of inequalities
	$y$ -intercept		

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### Materials List

Student journal  
Setting the Stage  
transparencies  
Dry-erase boards  
Markers and erasers

Scissors  
Chart paper  
Graphing calculators  
Calculator view screen  
Blank transparencies

Paper  
Lesson specific transparencies  
Overhead projector  
Construction paper  
Poster paper

The following table contains lesson name, timeline, summary of concepts covered, and the Essential Question(s) for each lesson.

Lesson	Timeline	Concepts Covered	Essential Question(s)	Common Core Standards for Mathematical Content
Plotting Points	1 Day	<ul style="list-style-type: none"> <li>• Coordinate plane and axes</li> <li>• Identify the four quadrants</li> <li>• Graph ordered pairs</li> <li>• Create a connected scatter plot on a grid and using technology</li> </ul>	How can you represent a table of ordered pairs visually?	5.G.1, 5.G.2, 7.G.1, 8.G.2, 8.G.3, G-MG.1, G-CO.2, G-CO.5, Modeling
Linear Equations in Slope-Intercept Form	2 to 3 Days	<ul style="list-style-type: none"> <li>• Linear functions represented five ways:               <ul style="list-style-type: none"> <li>○ Scenario</li> <li>○ Rule in words</li> <li>○ Rule as an equation</li> <li>○ Table of ordered pairs</li> <li>○ Graph</li> </ul> </li> <li>• Linear equations in slope-intercept form</li> <li>• Applications of linear equations in slope-intercept form</li> <li>• Graphic organizer related to lesson vocabulary</li> </ul>	How can a linear function represent a real-world scenario?	5.G.1, 5.G.2, 6.EE.9, 8.EE.6, 8.F.1, 8.F.2, 8.F.3, 8.F.4, 8.F.5, A-CED.2, A-REI.10, F-IF.4, F-IF.7a, F-BF.1, Modeling
Applications of Linear Functions in Slope-Intercept Form	1 to 2 Days	<ul style="list-style-type: none"> <li>• Determine linear equations from real-world scenarios</li> <li>• Determine linear equations given:               <ul style="list-style-type: none"> <li>○ Number pattern</li> <li>○ Polygon dot pattern</li> </ul> </li> <li>• Use linear equations to determine specific term value for various scenarios and patterns</li> </ul>	How does using a linear equation help answer questions related to linear patterns or scenarios?	5.G.1, 5.G.2, 6.EE.9, 7.EE.3, 7.EE.4a, 8.EE.6, 8.F.1, 8.F.2, 8.F.3, 8.F.4, 8.F.5, A-CED.2, A-REI.10, F-IF.4, F-IF.7a, F-BF.1, Modeling

Lesson	Timeline	Concepts Covered	Essential Question(s)	Common Core Standards for Mathematical Content
Linear Function Notation	1 Day	<ul style="list-style-type: none"> <li>Write equations using function notation</li> <li>For linear functions, determine:               <ul style="list-style-type: none"> <li>Domain</li> <li>Range</li> <li>Independent variable</li> <li>Dependent variable</li> </ul> </li> </ul>	How is function notation useful to represent linear function scenarios?	5.G.1, 5.G.2, 6.EE.9, 7.EE.3, 7.EE.4a, 8.F.1, 8.F.2, 8.F.3, 8.F.4, 8.F.5, A-CED.2, A-REI.10, A-REI.11, F-IF.1, F-IF.2, F-IF.4, F-IF.7a, F-BF.1a, F-LE.2, Modeling
Other Forms of Linear Functions	3 Days	<ul style="list-style-type: none"> <li>Standard form of a linear equation</li> <li>Point-slope form of a linear equation</li> <li>Determine linear equations that match real-world linear function scenarios</li> <li>Determine linear equations for horizontal and vertical lines</li> <li>Determine the equation of a line parallel or perpendicular to a second line and passing through a specific point</li> </ul>	What are the advantages of using linear equations to model linear functions and real world applications?	5.G.1, 5.G.2, 6.EE.9, 7.EE.4a, 8.EE.6, 8.F.3, A-CED.2, A-REI.10, Modeling
What is a Function?	1 to 1.5 Days	<ul style="list-style-type: none"> <li>Use the vertical line test to determine if a graph represents a function</li> <li>Graph various non-linear functions using a graphing calculator</li> <li>Create or match graphs that model real-world scenario. For example, distance-time graphs.</li> </ul>	What characteristic of a graph confirms that it can represent a function?	8.F.1, 8.F.2, 8.F.3, 8.F.4, 8.F.5, F-IF.1, F-IF.2, F-IF.4, F-IF.5, F-IF.7a, F-IF.7b, Modeling

Lesson	Timeline	Concepts Covered	Essential Question(s)	Common Core Standards for Mathematical Content
Linear Regression	2 Days	<ul style="list-style-type: none"> <li>Estimate the line of best fit for a set of data and then determine the slope-intercept form of the equation</li> <li>Use a formula to determine the correlation coefficient from a set of data</li> <li>Use a formula to determine the equation for the line of best fit</li> <li>Use the graphing calculator to determine the correlation coefficient and the equation for the line of best fit</li> <li>Make predictions based on the line of best fit</li> <li>Determine if a set of data has a linear trend based upon visual observations of the graph of data and the correlation coefficient</li> </ul>	How can linear regression be used to predict values and in real-world applications?	6.EE.9, 7.EE.4, 8.F.1, 8.F.2, 8.F.3, 8.F.4, 8.F.5, 8.SP.1, 8.SP.2, 8.SP.3, A-CED.2, A-REI.10, F-IF.1, F-IF.2, F-IF.4, F-IF.5, F-IF.7a, F-BF.1a, S-ID.6a, S-ID.6b, S-ID.6c, S-ID.7, S-ID.8, Modeling
Linear Inequalities	1 Day	<ul style="list-style-type: none"> <li>Graph linear inequalities by hand and using a graphing calculator</li> <li>Determine the linear equality from the graphed solution</li> <li>Graph the solution to a system of linear inequalities</li> <li>Apply linear inequalities to model and solve real-world problems involving two or more variables</li> </ul>	<ul style="list-style-type: none"> <li>How can the properties of inequalities be used to create a linear inequality in slope-intercept form?</li> <li>How can shading and dashed lines represent the solution to a linear inequality?</li> </ul>	6.EE.8, 7.EE.4b, A-CED.1, A-CED.3, A-REI.12, Modeling

## Systems of Equations

### Overview

All lessons are based on solving linear systems and include:

- Two Items One Table
- Two Items and a Diagram
- Balance Scales
- Systems of Equations and Tiles
- Solve Systems of Equations by Graphing

The number of total suggested days for the unit is 5 to 10. Adjustments may be needed based on student performance during the unit and amount of time available until the end of the semester.

### Vocabulary

Combination Table Situation	Mass Produce Represents Balance Scales	Systems of Equations Substitution Tiles	System Profit Operating Expenses
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### Material List

Student journal	Calculator view screen	Two bowls (5 cups or larger)
Setting the Stage transparencies	Blank transparencies	(optional)
Dry-erase boards	Lesson specific transparencies	Pitcher of Water (optional)
Markers and erasers	Overhead projector	Balance Scale (optional)
Overhead markers	Construction paper	Tiles
Graphing calculators	Poster paper	Tile pads

The following table contains lesson name, timeline, summary of concepts covered, and the Essential Question(s) for each lesson.

<b>Lesson</b>	<b>Timeline</b>	<b>Concepts Covered</b>	<b>Essential Question(s)</b>	<b>Common Core Standards for Mathematical Content</b>
Two Items One Table	2 Days	<ul style="list-style-type: none"> <li>• Create tables that represent the sum of multiple combinations for two different values</li> <li>• Determine an equation that represents the sum of multiple combinations for two different values</li> </ul>	How can a table be used to solve a system of equations?	6.EE.6, 6.EE.9, 7.EE.4, A-CED.2, Modeling
Two Items and a Diagram	2 Days	<ul style="list-style-type: none"> <li>• Use diagrams to determine unknown values (system of equations)</li> <li>• Use diagrams to work with the substitution concept of solving a system of equations</li> <li>• Use diagrams to work with combining two equations to solve a system of equations</li> </ul>	How can diagrams be used to solve a system of equations?	6.EE.6, 6.EE.9, 7.EE.4, 8.EE.8a, 8.EE.8b, 8.EE.8c, A-CED.2, A-REI.6, Modeling
Balance Scales	1 Days	<ul style="list-style-type: none"> <li>• Model a Systems of Equations using Balance Scales</li> <li>• Solve Systems of Equations using Balance Scales</li> </ul>	How can the concept of balance scales be used to solve a system of equations?	8.EE.8a, 8.EE.8b, 8.EE.8c, A-CED.2, A-REI.6, Modeling

Lesson	Timeline	Concepts Covered	Essential Question(s)	Common Core Standards for Mathematical Content
Systems of Equations and Tiles	1 Days	<ul style="list-style-type: none"><li>• Use tiles or blocks to represent a system of equations</li><li>• Develop a deeper conceptual understanding of solving a system of equations</li><li>• Solve system of equations with integers</li><li>• Solve system of equations by substitution</li><li>• Solve system of equations with rational and approximate rational solutions</li></ul>	How can tiles be used to solve a system of equations?	8.EE.8a, 8.EE.8b, 8.EE.8c, A-CED.2, A-REI.6, Modeling
Solve Systems of Equations by Graphing	2 Days	<ul style="list-style-type: none"><li>• Solve systems of equations by analyzing graphs and/or tables</li><li>• Solve one-variable equations by analyzing graphs and/or tables</li><li>• Model real world problems with graphs and tables</li><li>• Understand the links between algebra, tables, and graphs</li></ul>	How can graphing be used to solve a system of equations?	8.EE.8a, 8.EE.8b, 8.EE.8c, A-REI.6, A-REI.11, Modeling



# Non-Linear Functions

## Overview

The types of non-linear functions include:

- Quadratic functions
- Power functions
- Inverse variation functions
- Exponential functions
- Step functions
- Absolute value functions
- Circles (domain restricted to be a function)
- Piece-wise functions

The number of total suggested days for the unit is 18. Adjustments may be needed based on student performance during the unit and amount of time available until the end of the semester.

## Vocabulary

Square/squaring	Vertical line symmetry	Decay
Quadratic equation	Vertex	Exponential regression
Square root	$x$ -coordinate	Rise
Minimum point	$y$ -coordinate	Run
Maximum point	Quadratic regression	int() function
Standard form of a quadratic function	Multiples	Greatest integer
General form of a quadratic function	Power function	Floor function
Parabola	Even function	Smallest integer
Solutions	Odd function	Ceiling function
Quadratic formula	Direct variation	Binary number system
Discriminant	Inverse variation	Absolute value function
Double root	Constant of proportionality	Dilation
Break-even point	Base	Vertical line test
Symmetry	Exponent	General equation of a circle
	Exponential function	Piece-wise function
	Growth	

## Material List

Student journal	Blank transparencies	Construction paper
Setting the Stage transparencies	Lesson specific transparencies	Poster paper
Dry-erase boards	Overhead projector	Colored pencils
Markers and erasers		
Chart paper		
Graphing calculators		
Calculator view screen		

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## Planning Document

The following table contains lesson name, timeline, summary of concepts covered, and the Essential Question(s) for each lesson.

Lesson	Timeline	Concepts Covered	Essential Question(s)	Common Core Standards for Mathematical Content
Introduction to Quadratic Functions	1 Day	<ul style="list-style-type: none"> <li>Write and solve simple quadratic equations</li> <li>Use the graphing calculator to find vertex, <math>x</math>-intercepts, and to draw a graph</li> </ul>	How does the process of squaring relate to quadratic functions?	6.EE.9, 7.EE.4, 8.F.1, 8.F.2, 8.F.3, 8.F.4, 8.F.5, A-CED.2, F-IF.1, F-IF.2, F-IF.4, F-IF.5, F-IF.7a, F-IF.7c, F-BF.1a, Modeling
The Quadratic Formula	2 Days	<ul style="list-style-type: none"> <li>Standard form of a quadratic function</li> <li>Quadratic formula</li> <li>Discriminant</li> <li>Solve quadratic functions using the quadratic formula</li> <li><math>y</math>-intercept</li> <li>Applications of quadratic functions</li> </ul>	How can the quadratic formula be used to solve real-world applications?	6.EE.5, 6.EE.6, 6.EE.9, 7.EE.3, 7.EE.4, 8.F.1, 8.F.2, 8.F.3, 8.F.4, 8.F.5, A-CED.1, A-REI.1, A-REI.2, A-REI.5, A-REI.7, A-REI.10, Modeling
Graphing Quadratic Functions and Their Applications	3 Days	<ul style="list-style-type: none"> <li>Line of symmetry</li> <li>Vertex</li> <li>Graphing</li> <li>Applications of quadratic functions</li> <li>Quadratic regression</li> </ul>	How can quadratic functions and applications of quadratic functions be graphed?	6.EE.9, 7.EE.4, 8.F.1, 8.F.3, 8.F.4, A-APR.3, A-CED.2, A- REI.6, A-REI.7, A-REI.10, A-REI.11, F-IF.1, F-IF.4, F-IF.5, F-IF.7a, Modeling

Lesson	Timeline	Concepts Covered	Essential Question(s)	Common Core Standards for Mathematical Content
Power Functions	2 Days	<ul style="list-style-type: none"> <li>• Power function format</li> <li>• Odd and even functions</li> <li>• Graphing power functions</li> <li>• Transformations involving power functions</li> <li>• Applications of power functions</li> </ul>	Do power functions have patterns that can be used when solving and graphing them?	6.EE.9, 8.F.1, 8.F.2, 8.F.3, 8.F.4, 8.F.5, 8.EE.1, 8.EE.2, N-RN.2, A-CED.1, A-CED.2, A-REI.6, A-REI.10, F-IF.1, F-IF.2, F-IF.4, F-IF.5, F-IF.7, F-BF.3, Modeling
Inverse Variation	2 Days	<ul style="list-style-type: none"> <li>• Write equations involving direct variation</li> <li>• Constant of proportionality</li> <li>• Write equations involving inverse (indirect) variation</li> <li>• Graph direct and inverse variation</li> <li>• Identify inverse variation phrases</li> </ul>	<ul style="list-style-type: none"> <li>• How does inverse variation affect real-world application problems?</li> <li>• How does direction variation affect real-world application problems?</li> </ul>	6.RP.1, 6.RP.2, 6.RP.3, 6.EE.9, 8.F.1, 8.F.2, 8.F.3, 8.F.5, A-CED.2, A-CED.3, F-IF.1, F-IF.2, F-IF.5, F-IF.7d, F-BF.1a, Modeling
Exponential Functions	3 Days	<ul style="list-style-type: none"> <li>• Identify exponential functions</li> <li>• Growth and decay</li> <li>• Exponential applications</li> <li>• Graph exponential functions</li> </ul>	How do exponential functions behave in real-world applications?	8.EE.1, 8.F.1, 8.F.2, 8.F.5, N-RN.1, N-RN.2, A-CED.2, F-IF.1, F-IF.2, F-IF.4, F-IF.5, F-IF.7e, F-IF.8b, F-BF.1, F-LE.1c, Modeling

Lesson	Timeline	Concepts Covered	Essential Question(s)	Common Core Standards for Mathematical Content
Step Functions	2 Days	<ul style="list-style-type: none"> <li>• <i>Rise</i> and <i>run</i> of a step function</li> <li>• <i>Floor</i> step function</li> <li>• <i>Ceiling</i> step function</li> <li>• Graph step functions using the graphing calculator and the <b>int()</b> function</li> <li>• Applications involving step functions</li> </ul>	How do step functions apply to real-world applications?	8.F.1, 8.F.2, 8.F.5, F-IF.1, F-IF.2, F-IF.4, F-IF.5, F-IF.7, F-BF.1, Modeling
Miscellaneous Non-Linear Functions	3 Days	<ul style="list-style-type: none"> <li>• Absolute value functions               <ul style="list-style-type: none"> <li>○ Transformations involving absolute value functions</li> <li>○ Graph absolute value functions</li> </ul> </li> <li>• Circles               <ul style="list-style-type: none"> <li>○ Equations for circles</li> <li>○ Restrict domain of a circle equation</li> <li>○ Solve circle equations for <math>y</math></li> <li>○ Graph circle equations using center, radius, and intercepts</li> </ul> </li> <li>• Piece-wise functions               <ul style="list-style-type: none"> <li>○ Write piece-wise functions</li> <li>○ Graph piece-wise functions</li> <li>○ Applications of piece-wise functions</li> </ul> </li> </ul>	How do absolute value functions, piece-wise functions, and circle equations apply to real-world applications?	8.F.1, 8.F.2, 8.F.5, F-IF.1, F-IF.2, F-IF.4, F-IF.5, F-IF.7, F-BF.1, G-GPE.1, Modeling

# Probability and Statistics

## Overview

All lessons are based on probability and statistics. The probability and statistics lessons include:

- Fundamental Counting Principle
- Permutations and Factorial
- Combinations
- Probability
- Expected Winnings
- Parameters and Statistics

The number of total suggested days for the unit is 5 to 10. Adjustments may be needed based on student performance during the unit and amount of time available until the end of the semester.

## Vocabulary

Fundamental Counting Principle	Tree diagram	Without replacement	Mode
Permutation	Combinations	Expected winnings	Range
Factorial	Combination formula	Population parameter	Standard deviation
Standard form	Theoretical probability	Sample statistic	Lower quartile
Scientific notation	Experimental probability	Random sample	25 <sup>th</sup> percentile
Permutations formula	Independent event	Biased	Upper quartile
	Dependent event	Mean	75 <sup>th</sup> percentile
	With replacement	Median	Box and whisker plot

## Material List

Student journal	Graphing calculators	Construction paper
Setting the Stage transparencies	Calculator view screen	Poster paper
Dry-erase boards	Blank transparencies	Decks of cards (one for each group)
Markers and erasers	Lesson specific	Pennies
Overhead markers	Transparencies	Paper bags
	Overhead projector	

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## Planning Document

The following table contains lesson name, timeline, summary of concepts covered, and the Essential Question(s) for each lesson.

Lesson	Timeline	Concepts Covered	Essential Question(s)	Common Core Standards for Mathematical Content
Fundamental Counting Principle	1 to 2 Days	<ul style="list-style-type: none"> <li>Discover the Fundamental Counting Principle</li> <li>Use the Fundamental Counting Principle to determine the number of outcomes</li> </ul>	How can the Fundamental Counting Principle be used to determine the number of outcomes of an event?	7.NS.3, S-CP.1, Modeling
Permutations and Factorial	1 to 2 Days	<ul style="list-style-type: none"> <li>Use the Fundamental Counting Principle to determine the number of permutations possible for different situations</li> <li>Use the Fundamental Counting Principle to understand factorial</li> <li>Use factorials to define the calculations for permutations</li> <li>Determine the number of permutations for different situations</li> </ul>	<ul style="list-style-type: none"> <li>How can the Fundamental Counting Principle be used to define factorial</li> <li>How can factorials and permutations be used to determine the number of outcomes of an event?</li> </ul>	7.NS.3, S-CP.1, Modeling
Combinations	1 to 2 Days	<ul style="list-style-type: none"> <li>Use combinations to determine the total number of outcomes for lottery games</li> <li>Determine the number of combinations for different situations</li> </ul>	<ul style="list-style-type: none"> <li>How can combinations be used to determine the number of outcomes in gaming?</li> <li>How can combinations be used to determine the number of combinations of different situations?</li> </ul>	7.NS.3, S-CP.1, Modeling

Lesson	Timeline	Concepts Covered	Essential Question(s)	Common Core Standards for Mathematical Content
Probability	1 to 2 Days	<ul style="list-style-type: none"> <li>Determine the probability of independent and dependent events</li> <li>Determine theoretical and experimental probability</li> </ul>	<ul style="list-style-type: none"> <li>What is the difference between theoretical probability and experimental probability?</li> <li>How can the Fundamental Counting Principle, permutations, and combinations be used to determine probability?</li> </ul>	7.SP.5, 7.SP.6, 7.SP.7a, 7.SP.8a, 7.SP.8b, S-CP.1, S-CP.2, Modeling
Expected Winnings	1 to 2 Days	<ul style="list-style-type: none"> <li>Determine the expected winnings of different situations</li> </ul>	<ul style="list-style-type: none"> <li>How can probability be used to determine the expected winnings in various situations?</li> </ul>	7.SP.5, 7.SP.6, 7.SP.7a, 7.SP.8a, 7.SP.8b, S-CP.1, S-CP.2, S-CP.5a, Modeling
Parameters and Statistics	1 to 2 Days	<ul style="list-style-type: none"> <li>Determine the mean, median, mode, upper quartile, lower quartile, minimum, maximum, and standard deviation of a set of data.</li> <li>Draw a histogram</li> <li>Draw a box and whisker plot</li> <li>Investigate the difference between a population parameter and a sample statistic</li> <li>Investigate the relationship between a random sample and bias</li> <li>Investigate the spread of data and standard deviation</li> </ul>	<ul style="list-style-type: none"> <li>How is data used to create histograms and box and whisker plots?</li> <li>How are the various statistics used in real-world applications?</li> </ul>	6.SP.2, 6.SP.3, 6.SP.4, 6.SP.5, S-ID.1, S-ID.2, S-IC.1, S-IC.3, S-IC.4, Modeling